

HAMILTONIAN PATHS AND INDEPENDENCE TREE

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Abstract

Let $G = (X \cup Y, E)$ be a connected balanced bipartite graph of order 2n and vertex connectivity $\kappa(G)$ at least five. A spanning tree *T* of *G* (tree of *G* containing each vertex of *G*) is an independence tree, if the set of end vertices (vertices with degree one in *T*) is an independent set in *G*. If *G* has an independence tree *T*, then $\alpha_t^B(G, T)$ denotes the cardinality of the balanced set of end vertices in *T* and we define $\alpha_T^B(G)$ as the maximum $\alpha_t^B(G, T)$, for every independence tree *T* in *G*. In this paper, we show that if $\alpha_T^B(G) \leq \kappa(G)$, then between each pair of vertices *u* in *X* and *v* in *Y* there exists a Hamiltonian path (path of *G* containing each vertex of *G*).

Keywords and phrases: balanced bipartite graph, independence tree, vertex connectivity, Hamiltonian path.



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